A novel resistor-inductor network-based equivalent circuit model of lithium-ion batteries under constant-voltage charging condition

Jufeng Yang, Yingfeng Cai, Chaofeng Pan, Chris Mi

A constant-current constant-voltage (CCCV) charge protocol is commonly used for lithium-ion batteries. The dynamic characteristic of the constant-voltage (CV) charging current is discovered to be related to battery aging. In order to quantitatively describe the load current during the CV charging period, an equivalent circuit model (ECM) based on the resistor-inductor (RL) network is proposed in this paper. Motivated by the current expression derived based on the conventional resistor-capacitor (RC) network-based ECM, an RL network-based ECM is developed to characterize the CV charging current. Then, the parallel-connected RL networks are employed to improve the model fidelity. The test data of four lithium iron phosphate (LiFePO4) batteries in different aging states are employed to validate the proposed model. Comparative results show that the proposed 2nd-order ECM is the best choice, considering both the model accuracy and complexity. In addition, a simplified 2nd-order model is proposed, achieving a satisfactory accuracy with only three model parameters to be identified. Therefore, this model can be easily implemented in the battery management system (BMS).

1. Introduction

The transportation system is developing towards the electrification [1,2] and intelligence [3,4]. The success of vehicle electrification depends on the low-cost, safe and efficient on-board battery pack. Recently, lithium-ion batteries have been widely used in electric vehicles (EVs) due to their advantages of the long cycle life, high energy and power capabilities [5,6]. In order to ensure the safe and efficient operation, a sophisticated battery management system (BMS) is required to monitor and control the battery parameters such as voltage, current, state-of-charge (SoC) [7,8], state-of-health (SoH) [9,10], state-of-energy (SoE) [11] and so on, in real time. In the battery management
technique, the battery model is a basic issue for most of the state estimation algorithms. Hence, a simple yet accurate battery model is essential for a high-performance BMS.

1.1. Review of the literature

Due to the relatively simple structure and the satisfactory accuracy, the equivalent circuit model (ECM) is widely used for the on-board battery terminal voltage prediction and state estimation [12]. The conventional ECM consists of a finite number of resistor–capacitor (RC) networks connected in series. Specifically, the RC network is used to describe the polarization effects, and a higher number of RC networks (i.e., a higher order ECM) yields a higher degree of battery terminal voltage estimation accuracy [13,14]. However, at the same time, the complex model increases the computational burden and reduces the numerical stability for the subsequent battery state estimation, which limits its application on the low-cost microcontroller [15,16]. Different ECMs of lithium-ion batteries have been compared and analyzed in the literature by many authors. For example, Ref. [17] conducted a comparative study of twelve ECMS in terms of the model complexity, accuracy and robustness. Ref. [14] compared and analyzed seven impedance-based ECMS with respect to their voltage estimation and state-of-available-power prediction accuracy. Ref. [18] provided a comprehensive overview of the available battery/supercapacitor models, with a particular focus on fractional-order techniques. Besides, in order to decrease the computational effort without sacrificing the model accuracy, Ref. [19] simplified the complex ECM into the type of reduced order based on the dynamics of the battery. Additionally, a measurement noise model and data rejection were implemented to ensure the subsequent SoC estimation accuracy. Ref. [20] proposed an adaptive battery model based on a remapped variant of the Randles’ circuit model, and the subspace parameter-estimation algorithms were applied online and in combination with the battery state estimation. Experimental results demonstrated the superiority of this model to the conventional Randles’ circuit, in terms of the parameter identification and the states estimation performances. Ref. [21] developed an accurate battery model by considering the hysteresis dependence in the relationship between the open circuit voltage (OCV) and SoC, which ensured an accurate and stable SoC estimation. Ref. [22] employed the 1st-order ECM to estimate the battery SoC, and updated the model parameters online through the extended Kalman filter. Moreover, to reduce the convergence time, the initial states were determined by the recursive least squares algorithm and the off-line identification method.

It has to be noted that the ECMS within the aforementioned study are mainly used to predict the battery voltage response in the vehicle driving condition. For EVs, due to the dynamic and uncertain driving profile, the discharging process of the on-board battery tends to be incomplete and within a random SoC range. Hence, it is a challenging task to precisely evaluate the battery aging state, especially the capacity degradation, based on the driving profile [23]. However, it is more convenient for the BMS to estimate the battery SoH based on the relatively simple charging profile, such as the constant-current constant-voltage (CCCV) charging profile [24–26]. Abundant researches have been conducted to seek the accurate model for the battery under the CC charging condition. Tsang et al. [27] used a universal battery model based on a simple mathematical equation to capture the charging characteristics of the battery. The least squares algorithm was utilized to obtain the unknown model parameters. Verification results demonstrated that this model can capture the charging profiles at different charging rates. Furthermore, Low et al. [28] considered the influence of various ambient temperatures on this model, and developed a new temperature-based equation to represent the normalized CC charging profile at various ambient temperatures. Alifi et al. [7] trained the radial basis function network offline with the data collected from the battery charging process, then this kind of neural network was applied to determine the battery SoC. Compared with the constant-current (CC) profile, the constant-voltage (CV) profile is more robust to the uncertain initial charging state. In addition, the loss of lithium inventory occurred during the CC profile is more common and obvious than that occurred during the CC profile. Ning et al. [29] verified that 5.5% of the cyclable lithium loss took place in the CC charge mode but 94.5% cyclable lithium loss took place in the CV charge mode. These results confirmed that the measurements during the CV charging profile is effective to reflect the battery aging state. In order to quantitatively describe the dynamic characteristic of the current during the CV charging period, Eddahache et al. [30] used a simple exponential function based mathematical model to simulate the corresponding current behavior. In addition, they found that one of the identified model parameters was closely related to the battery capacity loss, and demonstrated a linear function with respect to the SoH. Yang et al. [31] and Wang et al. [32] obtained the detailed expression of the CV charging current based on the conventional first-order ECM, thus the associated parameters had the explicit physical meaning. Besides, two current-related characteristic parameters, i.e., the current time constant and the CV charging
aging factor, respectively, were further extracted to indicate the battery SoH. Although the estimated current in [31] can overall track the measured value, obvious mismatches were still observed at the initial and end regimes of the CV charging period.

1.2. Contributions of the paper

The objective of this manuscript is to seek a practical ECM that allows for accurate estimation of battery current under the CV charging condition. The main contributions of this paper are:

(1) A resistor-inductor (RL) network-based ECM is first introduced. The mathematical expression of the CV charging current is derived based on the conventional RC network-based ECM. According to the analysis of the expression, a novel ECM containing the RL network is proposed to characterize the battery current behavior though the CV charging period.

(2) Enhanced ECMs consisting of multiple RL networks are developed. Considering the nonlinear characteristic of the CV charging current, a higher order ECM with multiple RL networks connected in parallel are proposed to capture the current characteristic more precisely.

(3) A comparative study is conducted to determine the preferred model structure. The test data of four lithium iron phosphate (LiFePO4) batteries after different aging cycles are employed to validate the feasibility and superiority of the developed model. Comparative results demonstrate that the proposed 2nd-order ECM is the best choice, considering both the model accuracy and complexity.

(4) The simplified model is further developed. By analyzing the identified parameters of the 2nd-order ECM, a simplified model is proposed with satisfactory current estimation accuracy while with less parameterization effort in comparison to the same order ECM.

1.3. Organization of the paper

The reminder of this paper is organized as follows: In Section 2, the novel RL network-based ECM is introduced to characterize the CV charging current. In Section 3, the test procedure including the characterization tests and the aging tests are conducted based on four LiFePO4 batteries. In Section 4, the model parameterization method is presented, and the experimental results are performed to evaluate the performance of the proposed model. In Section 5, a simplified model is developed with satisfactory current estimation accuracy and less parameterization effort. Finally, some conclusions, the advantages of the proposed model, and the future work are given in Section 6.

2. Model development

2.1. RC network-based equivalent circuit model

The conventional ECM is mainly based on the RC network. Take the first-order ECM as an example, it is generally comprised of a voltage source \( V_{oc} \) an Ohmic resistance \( R_o \) and a RC network, which contains a resistance \( R_p \) and a capacitance \( C_p \) connected in parallel, as shown in Fig. 1.

Based on the Kirchoff’s law, the electrical behavior of the first-order ECM can be expressed as

\[
\begin{align*}
\frac{dV_r}{dt} + \frac{V_r}{R_p} &= I \\
V_{oc} + R_o I + V_p &= V_t
\end{align*}
\]

(1)

(2)

where \( V_r \) denotes the battery terminal voltage, \( V_p \) denotes the overvoltage across the RC network, and \( I \) denotes the load current (the positive value represents charging and the negative value represents discharging).

The battery terminal voltage is set as constant in the CV charging mode, while the charging current decreases continuously with time. In order to quantitatively describe the dynamic characteristic of the CV charging current, it is essential to derive the mathematical expression of the current in the CV mode. By substituting (2) into (1), the differential equation is rewritten as

\[
C_p \frac{d(V_t - V_{oc} - R_o I)}{dt} + V_t - V_{oc} - R_o I = I
\]

(3)

where \( V_{oc} \) denotes the open circuit voltage, and can be represented as a function of SoC, i.e.:

\[
OCV = f(SoC)
\]

(4)

where SoC can be further expressed as

\[
SoC(\tau) = SoC(0) + \eta \frac{\int I(t)dt}{3600 C_{cap}}
\]

(5)

where SoC(\tau) is the SoC at time \( \tau \), SoC(0) is the SoC at initial time, \( I(t) \) denotes the current at time \( t \), \( C_{cap} \) denotes the battery capacity in Ah, \( \eta \) denotes the coulombic efficiency, and \( \eta = 1 \) [11,33].

Based on (4) and (5), the variation of OCV with respect to time can be expressed as

\[
dOCV = dOCV/dSoC \cdot dSoC/dt = dOCV/dSoC \cdot \eta(I(t))/3600 C_{cap}
\]

(6)

where \( I(t) \) is usually lower than \( C/2 \) during the CV charging process, which means that the value of \( \eta(I(t))/3600 C_{cap} \) is generally less than 0.000139 in the CV mode. Hence, the value of \( dSoC/dt \) is very small, and \( dOCV/dt = 0 \) holds for the CV charging process.

Similarly, the variation of the impedance parameter can be considered negligible in the CV charging mode, i.e., \( dR_o/dt = 0 \). In addition, \( dV_r/dt = 0 \) can be obtained since the battery terminal voltage during the CV period is controlled constant.

Based on the aforementioned analysis, Eq. (3) can be simplified as

\[
\frac{dI}{dt} + \frac{R_o + R_p}{R_o R_p C_p} I = \frac{V_t - V_{oc}}{R_o R_p C_p}
\]

(7)

Assuming that \( V_t, V_{oc} \) and the impedance parameters (i.e., \( R_o, R_p \) and \( C_p \)) are all known variables, the detailed expression of the CV charging current can be solved as

\[
I(t) = I(0)e^{-\frac{R_o + R_p}{R_o R_p C_p}t} + \frac{V_t - V_{oc}}{R_o + R_p} \left(1 - e^{-\frac{R_o + R_p}{R_o R_p C_p}t} \right)
\]

(8)

where \( I(0) \) denotes the current at the beginning of the CV mode.

Defining \( R_o + R_p = a \) and \((R_o R_p C_p)/(R_o + R_p) = b \), Eq. (8) can be simplified as

\[
I(t) = I(0)e^{-\frac{t}{a}} + \frac{V_t - V_{oc}}{a} \left(1 - e^{-\frac{t}{a}} \right)
\]

(9)

2.2. The proposed equivalent circuit model for CV charging mode

For the system represented by (9), defining \( (V_t - V_{oc}) \) as the system
input and $I$ as the system output, Eq. (9) can be considered as the sum of the zero input response $y_1 = I(0)e^{-t/\tau}$ and the zero state response $y_2 = (V_i - V_{OC})/(1 - e^{-t/\tau})/a$. For the zero input response $y_1$, the value decreases exponentially to zero with time. For the zero state response $y_2$, the value increases exponentially from zero to the steady state $(V_i - V_{OC})/a$. It can be concluded from (9) that the variation rates of $y_1$ and $y_2$ are dependent on $b$, which can be considered as the time constant of the system. Based on the above analysis, Eq. (9) can be represented by an ECM containing one RL network, as shown in Fig. 2.

The electrical behavior of the proposed ECM can be expressed as

$$V_{OC} + ReqI + L_{eq}\frac{dI}{dt} = V_i$$

(10)

where $Req$ is the equivalent resistance and $L_{eq}$ is the equivalent inductance.

Based on the discussion in Section 2.1, $dV_{oc}/dt = 0$ holds for the CV charging mode, thus $I$ can be solved as

$$I(t) = I(0)e^{-t/\tau_{eq}} + \frac{V_i - V_{OC}}{Req} \left(1 - e^{-t/\tau_{eq}}\right)$$

(11)

where $\tau_{eq}$ is the equivalent time constant and $\tau_{eq} = L_{eq}/Req$.

By comparing (11) and (9), it is clear that the two equations have the same form when satisfying $a = Req$ and $b = \tau_{eq}$, proving the effectiveness of the proposed model structure. In addition, it can be concluded that the proposed ECM shown in Fig. 2 contains less components compared with the conventional one shown in Fig. 1, which in turn leads to a lower parameterization effort.

For the CV charging mode, the battery terminal voltage remains constant, while the load current decays nonlinearly with time, causing the concentration gradient of lithium ions to decrease progressively to a slight level when the CV charge ends [29,30]. Hence, the CV charging current is closely related to the nonlinear electrochemical processes occurred inside the battery. It can be concluded from (11) that the dynamic characteristic of the CV charging current is mainly determined by the time constant of the RL network. However, the estimated current obtained based on the ECM shown in Fig. 2 cannot closely track the measured value, which will be discussed in Section 4.2. In the conventional ECM, the RC network is widely adopted to approximate the nonlinear polarization effects in the time domain, and a higher number of RC networks with different time constants are generally connected in series to give a better approximation [34]. Hence, in order to accurately describe the dynamic characteristic of the CV charging current, exponential functions with different time constants are employed together to reproduce the battery electrochemical processes. Correspondingly, the proposed ECM shown in Fig. 2 can be extended to a higher order with multiple RL networks connected in parallel, as shown in Fig. 3.

For the ECM shown in Fig. 3, the equation of the branch current through each RL network are similar to (11). In addition, according to Kirchoff’s current law, the sum of branch currents flowing into the node, i.e., point A in Fig. 3, is equal to the value of the total charging current. Hence, the detailed expressions of each branch current and the associated relationships are

$$\begin{align*}
    l_k(t) &= I(0)e^{-t/\tau_{eq,k}} + \frac{V_i - V_{OC,k}}{Req,k} \left(1 - e^{-t/\tau_{eq,k}}\right), \\
    \sum_{k=1}^{n} l_k(t) &= I(t)
\end{align*}$$

(12)

where $n$ is the order of the model, $l_k(t)$ denotes the branch current through each RL network, $Req,k$ and $\tau_{eq,k}$ denote the equivalent resistance and the equivalent time constant for each RL network, respectively.

### 3. Experimental tests

#### 3.1. Experimental setup

The batteries employed in this study are four 26,650 power cells, which are numbered from #1 to #4. Four batteries are stimulated with the same load current or power profiles for comparison and validation. The key specifications of the investigated battery are listed in Table 1.

The tests are conducted on an 8-channel Arbin BT2000 battery cycler with a voltage range of 0–5 V and a current range of −100 to 100 A. The voltage and current accuracy is ±0.02% for low power and ±0.05% for high power applications. All four batteries are placed in an air-conditioned room with a temperature range of 25 ± 2 °C, and the sampling frequency of the data acquisition is set as 1 Hz.

#### 3.2. Test procedure

The battery test procedure consists of two parts, i.e., the characterization tests and the aging test. The objective of the characterization tests is to obtain the batteries’ capacity and SoC-OCV correlation, so as to identify the impedance parameters of the ECM derived in Section 2.2. The aging test is utilized to cycle the investigated batteries to different aging states.

##### 3.2.1. Characterization tests

In order to extract the battery information at different aging states, the characterization tests are conducted after a certain number of aging tests. The characterization tests in this study are composed of two parts: the capacity test and the hybrid pulse power characterization (HPPC) test.

The capacity test includes 5 charge-discharge cycles. In each cycle, the battery is first charged at a constant current of 0.5C rate until the battery terminal voltage reaches the cut-off value of 3.65 V, then a CV mode is applied until the charging current reaches the cut-off value of C/20. After resting for 1 h, the battery is discharged in a CC mode at 0.5C rate until the battery terminal voltage reaches 2.0 V. The rest period between two cycles is 1 h. Finally, the battery’s capacity is calculated as the mean value of the accumulative charge of 5 cycles.

It can be inferred from (12) that the input variable of the system contains the battery OCV, which should be determined in advance. In this study, the SoC-OCV correlation is obtained by the HPPC test. In the HPPC test, the battery is first stimulated with a pair of discharge and charge current pulses, with the amplitude of 2C and the duration of 10 s. Then, after resting for 60 s, the battery is incrementally discharged/charged with the interval of 5% SoC at a constant current of 0.5C rate, this is followed by a 2 h relaxation period to reduce the polarization effects.

##### 3.2.2. Aging tests

After the characterization tests, the investigated batteries are cycled in the aging test. In each aging cycle, all four batteries are charged at a constant current of 1C rate until the charge cut-off voltage (3.65 V) is reached, then the CV charging mode is conducted until the current reduces to C/20. After that, the batteries are discharged immediately in a CC mode at 4C rate to the discharge cut-off voltage (2.0 V).

![Fig. 2. Proposed RL network-based ECM.](image-url)
In spectively, and to the start point and the end point of the CV charging process, re- 

4. Model parameterization and veri 

The time-current series acquired during the CV charging period are 

in the obtained estimation errors, as shown in Fig. 4(b), (d), (f) and (h), 

4.2. Model veri 

In order to verify the feasibility of the proposed model, the obtained RMSE and R² of battery #2 at different aging states. The obvious reduction of RMSE and increase of R² are observed from the 1st-order ECM to the 2nd-order ECM. By contrast, the variations of the evaluation criterions are much smaller from the 2nd-order ECM to the 3rd-order ECM. These phenomena are in accordance with the estimation results depicted in Fig. 4. In addition, it can be seen from Fig. 5(b) that both the R²’s of the 2nd-order ECM and the 3rd-order ECM are close to 1, indicating the high current estimation accuracy of these two models.

In order to further verify the applicability of the proposed model, the obtained RMSE and R² of battery #2, #3 and #4 are listed in Table 2. As can be seen, the aging states of all three batteries have no significant influence on the estimation accuracy of the proposed ECMs. In addition, the parameters identified from one battery (battery #1) can be applied to estimate the charging current of other three batteries with satisfactory performance. Besides, it can be found from Table 2 that the model accuracy is closely related to the model structure. Take battery #2 as an example, for the 2nd-order model, the RMSE is reduced by approximately 75.4% overall and with 3 more model parameters in comparison to the 1st-order model. Moreover, the overall RMSE is only reduced by approximately 10.5% from the 2nd-order model to the 3rd-order model, but the model parameters are increased from 5 to 8. This phenomenon can also be verified by the estimation results of battery #3 and battery #4. It can be concluded that the higher number of RL networks leads to the better current estimation performance; however, at the expense of the higher parameterization effort. Hence, considering the tradeoff between the model fidelity and the parameterization effort, the proposed 2nd-order ECM is the best choice to characterize the CV charging current.

On the other hand, the mathematical function proposed in Ref. [30] is also conducted to make a comparison. Specifically, the mathematical function is expressed as

\[ I(t) = Ae^{-Bt} + C \]  

where A, B and C are the function coefficients, which can be identified by the NLS algorithm described in Section 4.1.

Table 3 shows the calculated evaluation criterions of the current estimation results by (16). By comparing Tables 2 and 3, it demonstrates that for all three tested batteries, the proposed ECM containing more than one RL network can provide more accurate estimated current, which further proves the superiority of the proposed ECM in terms of the estimation accuracy.

5. Model simplification

Based on the aforementioned analysis, it can be concluded that the proposed ECM containing 2 RL networks can ensure the sufficient accuracy of current estimation. Table 4 gives the identified model parameters for battery #1 at different aging states.

According to (12), it is clear that the values of \((V_i - V_{\infty})\) and \(R_{eq,k}\)
directly influence the zero state current response. The value of $V_{oc}$ is generally close to the battery terminal voltage during the CV charging mode, leading to a low $(V_t - V_{oc})$ value (approximate 0.296 V). It can be observed from Table 4 that the estimated equivalent resistances, especially $R_{eq,2}$, possess relative high values. Hence, the $(V_t - V_{oc})(1 - e^{-t/\tau_{eq,k}})/R_{eq,k}$ part in the estimated current can be neglected, which means that the fitting function of the 2nd-order ECM can be simplified as

$$I(t) = I_1(0)e^{-\frac{t}{\tau_{eq,1}}} + [I(0) - I_1(0)]e^{-\frac{t}{\tau_{eq,2}}} \tag{17}$$

It can be found from (17) that only three model parameters are required to be identified, i.e., $I_1(0)$, $\tau_{eq,1}$ and $\tau_{eq,2}$.

In order to assess the performance of the simplified model, Fig. 6 shows the estimation results and the absolute values of errors at different aging states. Specifically, the model parameters are identified based on the test data of battery #1, and the estimation results based on the test data of battery #2 are demonstrated as examples. In addition, the evaluating criterions of battery #2, #3 and #4 are listed in Table 5. As can be seen, the estimated current curve matches well with the measured results at different battery aging states. By comparing Tables 2 and 5, it can be observed that the current estimation accuracy is slightly decreased from the 2nd-order model to the respective simplified one, due to the neglect of the $(V_t - V_{oc})(1 - e^{-t/\tau_{eq,k}})/R_{eq,k}$ ($k = 1$ and 2) part. Compared with the 1st-order model, the estimation accuracy of the simplified model is significantly improved with the same number of model parameters. Hence, it can be concluded that for the
simplified 2nd-order model, the number of model parameters is reduced, yet the current estimation accuracy can still be guaranteed.

6. Conclusion

A novel RL network-based ECM is proposed in this paper, which can capture the dynamic characteristic of the charging current at CV mode. According to the current expression derived upon the conventional RC network-based ECM, a battery ECM containing one RL network is first introduced. Secondly, in order to improve the model fidelity, the proposed model is generalized to a higher order with multiple RL networks connected in parallel with each other. Thirdly, based on the analysis of the identified model parameters, a simplified 2nd-order model is developed to decrease the parameterization effort. Lastly, the NLS algorithm is employed to identify the model parameters, and four LiFePO4 batteries are tested to validate the proposed model. Comparison results indicate that a higher number of RL networks lead to a more accurate current estimation, however, at the expense of higher parameterization effort. Besides, the simplified 2nd-order model can be a good candidate considering the tradeoff between the model accuracy and complexity.

The proposed model has several advantages desired for the BMS. First, it contains less parameters compared to the conventional RC network-based ECM with the same order, and thus requires a lower parameterization effort. For the simplified model, this superiority is enhanced since the number of identified model parameters is further reduced. In addition, due to the electrical characteristic of the RL network, the proposed model can capture the dynamics of the CV charging current precisely. According to our previous work [31], the dynamic characteristic of the charging current during the CV period is closely related to the battery aging state. Hence, with the proposed model, it is possible to explore an effective way to estimate the battery SoH.

In this paper, only LiFePO4 batteries are adopted in the test, and the test temperature is maintained around 25°C. Hence, future work will be focused on verifying the proposed model with different battery chemistries at different temperatures. In addition, a novel battery SoH estimation method based on the developed model will be presented.

Acknowledgements

The authors would like to acknowledge the funding support from

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Table 2
Calculated evaluation criteria of the current estimation results by the proposed ECMs.
the National Science Foundation, US (1507198); the National Natural Science Foundation of China (51875255, U1664258); and the Natural Science Foundation of Jiangsu Province (BK20171300).

References


