Ecological Driving System for Connected/Automated Vehicles Using a Two-Stage Control Hierarchy

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Abstract—To improve a vehicle’s fuel efficiency when operating on roadways, this study develops an ecological driving system under the connected and automated vehicle (CAV) environment. The system includes three critical functions, including traffic state prediction, eco-driving speed control, and powertrain control implementation. According to the real-time traffic information obtained from vehicle-to-infrastructure and vehicle-to-vehicle communications, the embedded traffic state prediction model will estimate and predict the average speeds and densities of freeway subsections. With an objective of minimizing the fuel consumption, the eco-driving speed control function follows a two-stage hierarchical framework. The first stage, which is executed at the global level, aims to optimize the travel speed profile of the CAV over a certain time period. The second stage, local speed adaption, is designed to dynamically adjust the CAV’s speed and make lane-changing decisions based on the local driving condition. The resulting control parameters will then be forwarded to the powertrain control system for implementations. To evaluate the proposed system, this study performs comprehensive numerical tests by using simulation models. This results confirm the effectiveness of the proposed system in reducing fuel consumption. Further comparisons with different models highlights the need to consider traffic state information in the first-stage optimization and lane-changing decision module in the local adaption function.

Index Terms—Eco-driving, connected and automated vehicle (CAV), traffic state prediction, fuel consumption minimization, two-stage control hierarchy.

I. INTRODUCTION

According to the U.S. Department of Transportation (USDOT) surveys, transportation sector consumes 28% of total energy to move people and goods in the United States [1]. Despite the existence of many transportation modes such as personal cars, buses, trucks, trains, airplanes, and ships, so far the largest share of energy consumption is from cars and light trucks [2]. Hence, improving vehicle’s fuel efficiency becomes a vital issue in transportation engineering. Although drivers’ behaviors are commonly recognized as one of the most important factors [3] that affects energy consumption, the design of powertrain operational systems also play a key role in improving fuel efficiency.

In response to such a need, a large amount of studies have reported their methodologies to design ecological driving system, which aims to operate vehicles in an energy efficient way. Early studies developed the so called “eco-cruise control” system which dynamically adjust cruise speed based on the roadway grade information [4]. To operate vehicles in a more complex environmental, more recent studies focused on the design of eco-oriented driving systems which can optimize vehicle speed profile in real time. The most pioneer works in such field have been conducted on single vehicles. Notably, some field experiments have highlighted the potential benefits of eco-driving systems on reducing vehicles’ fuel consumption [5]–[9]. In review of the literature, a group of researchers developed a set of speed optimization algorithms that allow vehicles to adjust their travel speeds within a specified range [10], [11]. By accounting for the topography information, those systems enable vehicles to use the energy gained from downhill roadway sections to overcome the grade resistance on uphill sections. Similarly, another group reported their algorithms in optimizing vehicle trajectories [12], [13] and several studies extended the control logic to heavy vehicles [14]. However, these aforementioned studies may fall short of effectiveness due to the lack of real-time traffic information.

Recent technology advancement on connected and automated vehicles (CAVs) provides the possibility of integrating real-time traffic information into an eco-driving system. With on-board communication devices, connected vehicles are allowed to exchange information with other vehicles (V2V), roadside infrastructure (V2I), and the “Cloud” (V2C). Fully automated vehicles are defined by National Traffic Safety Administration (NHTSA) as those in which operation of the vehicle occurs without direct driver input to control the steering, acceleration, and braking and are designed so that the driver is not expected to constantly monitor the roadway while operating in self-driving mode. Using CAV technologies, existing studies have reported various models to improve the efficiency of eco-driving systems. According to [15], those studies can be classified into two categories: vehicle speed/acceleration control and powertrain control. The first
category of studies aimed at optimizing the speed profile and acceleration rate so as to minimize the fuel consumptions. Those optimization models are developed with various control objectives such as intelligent merging [16], [17], platooning [18]–[20], and eco-approaching [21], [22]. The second category focused on the real-time optimization of key parameters in vehicles powertrain system [23]–[25] where regular vehicles, electric vehicles, and hybrid vehicles are all studied by various researchers.

After obtaining the real-time information, it is always critical to explore efficient computational algorithms in the optimization process since CAVs need to be safely operated in response to the change of travel environment. A group of researchers used dynamic programming (DP) as the tool to solve the nonlinear models with complex constraints [26], [27]. While DP was proven to be effective, its computation time is still too long for real-time operations. To overcome this issue, other studies developed Model Predictive Control (MPC) with quadratic programming technique [28] and Legendre Pseudospectral method [29]. However, those approaches are only capable of dealing with a relatively short time horizon due to limitations caused by the computational efficiency requirement. The short horizon, which can satisfy the on-line operation need, generally produces less optimized solution from the long-term aspect.

To fully account for the benefit of long-term optimization and the computation efficiency of short-term operations, reference [30] developed a two-stage hierarchy in designing distance-based ecological driving system. Using the speed limit as the target speed, the first stage of their control framework, named “long-term optimization”, is used to find the most energy-efficient speed profile between the vehicle’s origin and destination. Such optimization is done before the departure of vehicles. Then based on the obtained speed profile, the second stage named “local adaptive” is used to dynamically adjust vehicle’s speed according to real-time driving condition (e.g., the speed and location of nearby vehicles). Despite the effectiveness of such two-stage control hierarchy in reducing energy consumption, the entire optimization process is operated with a single vehicle and real-time traffic condition is not taken into account.

In this study, we will explore the potential of introducing vehicle automation and connectivity into the two-stage hierarchy. The main contributions of this work are summarized as follows: 1) developing an eco-CAV operational framework which allows the target CAV to take into account real-time traffic information for powertrain optimization; 2) integrating traffic state prediction function and implementing such information with a rolling-horizon control logic; and 3) providing a lane-changing decision function in the local adaptation stage to further improve fuel efficiency.

The remaining of this paper is organized as follows. Section II will introduce the CAV operational environment and illustrate the control framework of the proposed eco-driving system. Section III will present the details of model formulation in the three key steps: traffic state prediction, long-term speed profile optimization, and local adaption. Section IV will show the system evaluation with numerical examples and Section V will conclude the paper.

II. ECOLOGICAL DRIVING SYSTEM ARCHITECTURE

A. CAV Operational Environment

The connectivity technology of CAVs allows the exchange of traffic information between vehicles and infrastructure. The vehicle automation function will automatically adjust the speed in real time through the optimization of the powertrain system. As shown in Fig. 1, roadside traffic sensors are able to collect the traffic data such as flow rate (number of vehicles) and average vehicle speed. Through the communication infrastructure, data from multiple neighboring sensors will be recorded and sent to CAVs (V2I). Then the computational devices on CAVs can perform computational works based on the real-time data. For the need of vehicle automation, it always requires reliable sensors on automated vehicles. Three major types of sensors are used in practice, including radar, LiDAR, and camera. With the integration and coordination of different types of sensors, the automated vehicles can be aware of the locations and speeds of surrounding vehicles. Such detected information can be further sent to other nearby CAVs through the V2V communication platform. By integrating the connectivity technology with vehicle automation, the proposed ecological driving system in this study can guarantee its operational effectiveness even with a low penetration rate of CAVs.

B. Proposed System Architecture

Fig. 2 shows an overview of the proposed two-stage eco-driving optimization framework. The traffic state model will
yield a prediction of the freeway traffic condition using real-time traffic information. Let $S$ denote the total travel distance between the target CAV’s origin and destination, and $n$ denote the number of distance segments. At any given time $t$, the traffic state model predicts the average traffic speed profile for each of the $n$ distance steps $\hat{V}(s, t) = [\hat{V}(s_1, t), \ldots, \hat{V}(s_n, t)]$, where $\hat{V}(s_i, t)$ denotes predicted average traffic flow speed at the $i$-th distance segment and $s_i$ denotes the $i$-th distance segment. The advantage of using $\hat{V}(s, t)$ as the reference in our model is twofold: first, average traffic flow speed profile prediction allows us to consider realistic traffic condition, whereas considering only speed limit on a specific road section for optimization would result in too optimistic speed profile and cause abrupt speed reductions when local adaption is performed; second, the prediction model takes into account time-varying traffic state. As will be shown later, by using the rolling horizon control logic, we can periodically refresh the predicted speed profile $\hat{V}(s, t)$ to take into account the most up-to-date traffic state information.

The predicted real-time traffic speed profile is then communicated to the CAV through V2I channel and will be used as input information for long-term global eco-driving optimization, as illustrated in Step 2 of Fig. 2. In this step, the system optimizes powertrain control parameters such as engine torque and brake force with an objective of minimizing vehicle’s fuel consumption. Several constraints, such as speed constraints derived from previously estimated global average speed profile $\hat{V}(s, t)$ and road conditions, etc. are taken into account. The optimized powertrain control parameters will be further used to compute the speed profile on each of the $n$ distance steps: $V_{opt}(s, t) = [V_{opt}(s_1, t), \ldots, V_{opt}(s_n, t)]$. Details on global long-term optimization will be discussed in Section III-B.

The second step of the two-stage hierarchical framework is dynamic local speed adaption, which uses optimized long-term speed profile $V_{opt}(s, t)$ as a reference in the optimization, as shown in Step 3 of Fig. 2. However, during the course of driving, unpredictable events may interrupt driving and prevent the vehicle from following long-term speed profile. For example, preceding neighboring vehicles from other lanes may suddenly change to the CAV’s lane and consequently result in potential traffic accidents. In this case, it is critical to dynamically adapt the instantaneous speed profile to maintain safety distance. Thus, during local adaption, optimization is performed repeatedly by taking into account local road perturbations and safety driving distance as dynamic constraints. More details on local adaption will be discussed in Section III-B. In the following section, we will discuss details of constituent blocks in the proposed system architecture.

### III. Model Development

In this Section, we will show the details of our eco-driving model. Table I provides a summary of vehicle and model parameters considered in this manuscript.
A. Traffic State Prediction

The first step of the proposed system is the prediction of current traffic state. To provide traffic state (speed and density) as input to the two-stage eco-driving control hierarchy, it is essential to predict the traffic state evolution on the target roadway sketched over a projected time horizon. In this work, we employ a macroscopic traffic flow model to predict the flow rate, average speed, and density. As discussed before, the target roadway segment is divided into \( n \) segments with a unit length of \( \Delta s = S/n \). When dividing a freeway segment, the length of each segment should be sufficiently long so that vehicles cannot pass one subsection during one time interval. Moreover, each subsection is allowed to have at most one on-ramp and one off-ramp. For the \( i \)-th segment at a given time \( t \), the mean density \( D_i(t) \) can be determined by the difference between the input and output flows as follows:

\[
D_i(t+1) = D_i(t) + \frac{\Delta T}{\Delta s} \times n_i [q_i(t) - q_{i-1}(t) + r_i(t) - s_i(t)]
\]

(1)

where \( q_i(t) \) denotes transition flow rate entering segment \( (i + 1) \) from segment \( i \) at \( t \), \( r_i(t) \) denotes the on-ramp flow rate entering segment \( i \) at \( t \), \( s_i(t) \) denotes the off-ramp flow rate leaving segment \( i \) at \( t \), \( n_i \) is the total number of lanes, and \( \Delta T \) denotes the unit time interval to update the traffic flow model. The transition flow rate is determined by:

\[
q_i(t) = D_i(t) \times \hat{V}(s_i, t) \times n_i
\]

(2)

To dynamically update the average speed, \( \hat{V}(s_i, t) \), a well-developed equation proposed by [31] in their METANET model is adopted and shown as follows:

\[
\hat{V}(s_i, t+1) = \hat{V}(s_i, t) + \frac{\Delta T}{\tau} [V[D_i(t)] - \hat{V}(s_i, t)]
\]

\[
- \frac{\Delta T}{\Delta s} \hat{V}(s_i, t) \{ \hat{V}(s_i-1, t) - \hat{V}(s_i-1, t+1) \}
\]

\[
- \frac{V \cdot \Delta T}{\tau \cdot \Delta s} D_{i+1}(t) - D_i(t)
\]

(3)

where \( V[D_i(t)] \) is the static speed for segment \( i \) at time \( t \) with respect to the density:

\[
V[D_i(t)] = \frac{\nu \cdot \tau \cdot \kappa}{\alpha} \exp\left(-\frac{1}{\alpha} \left(\frac{D_i(t)}{D_c}\right)^\alpha\right)
\]

(4)

and \( \nu, \tau, \kappa, \alpha \) are traffic state model parameters and \( D_c \) is the critical density. Using the macroscopic traffic flow model (Eqs. 2-4), the system can predict the average speed of each sub-segment \( i \) over projected time horizon. Since the model is implemented with an assumption that the detected traffic flow pattern remains unchanged overtime, the long-term prediction may not be accurate enough for applications when the distance between vehicle’s origin and destination is long. Hence, instead of performing a one-time traffic prediction before the departure of vehicle, this study employs the rolling-horizon control logic in the eco-driving system. As shown in Fig. 3, a long-term prediction will be carried out before the departure of vehicle and the resulting traffic state (#1) will be implemented as the input of two-stage hierarchy model. Once the vehicle approaches a new communication infrastructure, new data from traffic sensors will be available through V2I communication. At this time, another traffic state prediction based on updated data will be executed and the new traffic state (#2) will be used as input. Such procedure will be repeated until the vehicle reaches its destination. By using the rolling-horizon framework, the proposed eco-driving system can fully take advantage of the benefit of CAV technology and utilize most updated information for optimization.

B. Long-Term Optimization

The predicted traffic flow will then serve as the baseline for our two-stage hierarchical model to minimize fuel consumption under various traffic condition constraints. The goal is to dynamically estimate control of powertrain parameters in order to minimize fuel consumption based on several considerations: i) average traffic flow profile derived from our traffic state prediction model ii) speed constraints and road conditions, iii) neighboring vehicle distance and speed.

1) Fuel Consumption Formulation: The long-term optimization serves as global model to estimate most energy-efficient powertrain control states for a predefined traveling distance, denoted by \( S \). The optimization takes into account average traffic flow speed profile derived from our traffic state prediction model \( \hat{V}(s, t) = [\hat{V}(s_1, t), \ldots, \hat{V}(s_n, t)] \).

Specifically, the fuel consumption cost given a time window \([t_0, t_f]\) can be expressed as shown in [24]:

\[
J = \int_{t_0}^{t_f} \dot{m}_f(t)dt
\]

(5)

where \( \dot{m}_f(t) \) denotes instantaneous mass fuel rate (kg/s) which is a function of powertrain control input vector \( \vec{u}(t) = [T_e(t), \omega_e(t)] \), where \( T_e \) is the engine torque and \( \omega_e \) is the engine rotational speed. In this work, we adopt Willans line approximation [32] for expressing \( \dot{m}_f(t) \) and use the distance-based fuel consumption expression in [30] to further express \( J \) as:

\[
J = \sum_{k=0}^{n-1} \left( \beta_1 f_r g_r(n_r/r_w) + \beta_2 \cdot T_e(k) \right) \Delta s
\]

(6)

where \( \beta_1 = 5.646 \times 10^{-8}, \beta_2 = 4.751 \times 10^{-7}, \gamma_1 = 1.625 \times 10^{-6}, \gamma_2 = -5.968 \times 10^{-5}, v(k) \) denotes vehicle velocity (m/s) at k-th segment, \( r_w \) denotes wheel radius, \( f_r \) is
the final drive ratio and \( g_r(n_r) \) is the gear ratio given a gear number \( n_r \), which is determined by the gear shifting rules as specified in Fig. 4, and \( \Delta s \) is the distance of each segment: \( S = \Delta s \times n \). According to [30], the state equation for the speed at \( k \)-th segment can be expressed as:

\[
\nu(k)^2 = (1 - \frac{2C_2\Delta s}{m})\nu(k-1)^2 + \frac{2C_1\Delta s}{m} - \frac{2C_3\Delta s}{m} \left( T_e(k-1) \right) - \frac{2C_3\Delta s}{m} \]

(7)

where \( m \) denotes the mass of the vehicle (kg), \( F_{\text{brake}} \) denotes the brake force applied at one segment, \( C_1, C_2 \) and \( C_3 \) are vehicle parameters defined as:

\[
C_1 = \frac{f_r g_r(n_r) N_{fr} N_{gr}(n_r)}{r_w} \]

(8)

\[
C_2 = \frac{1}{2} \rho C_D A_d \]

(9)

\[
C_3 = m \cdot g \cdot C_r \cos \theta(k) + m \cdot g \cdot \sin \theta(k) \]

(10)

where \( N_{fr} \) denotes the efficiency of the final drive, \( N_{gr}(n_r) \) denotes the efficiency of a gear box and a torque converter which is a function of the gear number, an input speed, and an input torque, and it is modeled as the product of the gearbox efficiency and the torque converter efficiency, \( \rho \) denotes the air density (kg/m\(^3\)), \( C_D \) denotes the drag coefficient, \( A_d \) denotes the frontal area of the vehicle (m\(^2\)), \( g \) is the gravity (m/s\(^2\)), \( C_r \) is the rolling resistance coefficient, and \( \theta(t) \) is the road grade (rad). For a given vehicle and a predefined traveling distance, assume that the initial velocity is \( \nu(0) \), and let the vector \( U \) denote the powertrain control parameters applied on all segments of the entire traveling distance: \( U = [T_e(0), F_{\text{brake}}(0), \ldots, T_e(n-1), F_{\text{brake}}(n-1)] \), then the fuel consumption optimization search algorithm consists of computing the optimal value of \( U_{\text{opt}} \) in the \( (2 \times n) \)-dimensional space that minimizes the total fuel consumption \( J \).

2) Fuel Consumption Optimization With Constraints: In order to consider velocity profile as our optimization constraints, we need to express velocity as a function of our optimization parameter vector \( U \). In this work, we use the expression shown in [30] to rewrite equation (7) as:

\[
X(k + 1) = A(k)X(k) + B(k)u(k) - D(k) \]

(11)

where \( X(k) = (\nu(k))^2 \), \( A(k) = 1 - \frac{2C_2\Delta s}{m} \), \( B(k) = \left[ \frac{2C_1\Delta s}{m}, -\frac{2C_3\Delta s}{m} \right] \), \( u(k) = [T_e(k), F_{\text{brake}}(k)]^T \), \( D(k) = \frac{2C_3\Delta s}{m} \).

Then the vehicle longitudinal states for all segments can be expressed in matrix form as shown in (12), as shown at the bottom of this page.

We can then use matrix notations \( \tilde{A}, \tilde{B}, U, \tilde{C} \) and \( D \) to rewrite Equation (12):

\[
X = \tilde{A}X(0) + \tilde{B}U + \tilde{C}D \]

(13)

We can manipulate equation (13) as the following:

\[
\tilde{B}U = X - \tilde{A}X(0) - \tilde{C}D \]

(14)

Equation (14) allows us to impose linear equalities to global fuel consumption optimization based on predicted average traffic speed profile \( \hat{V}(s,t) \). The global fuel consumption optimization can be then formulated as following:

\[
\min_U \sum_{k=0}^{n-1} \left( \beta_1 \frac{f_r g_r(n_r)}{r_w} + \beta_2 \right) T_e(k) + \gamma_1 \frac{f_r g_r(n_r)}{r_w} + \gamma_2 \Delta s \]

subject to \( 0 \leq U \leq U_{\text{max}} \)

\[
\begin{bmatrix}
-\tilde{B} \\
\tilde{B}
\end{bmatrix} U \leq \begin{bmatrix}
-(X_{\text{min}} - \tilde{A}X(0) - \tilde{C}D) \\
X_{\text{max}} - \tilde{A}X(0) - \tilde{C}D
\end{bmatrix}
\]

(15)

where \( U_{\text{max}} \) denotes the upper boundary of powertrain control parameter. \( X_{\text{min}}/X_{\text{max}} \) is speed lower/upper boundary. The global optimization formulated in (15) provides optimal...
powertrain control that minimizes fuel consumption for a given driving distance $S$ by taking into account road condition and predicted global traffic speed profile. Note that global traffic speed profile is dynamically predicted and can be updated periodically to reflect global traffic flow change. In such case, global optimization formulated in (15) is also performed periodically using rolling horizon control logic to ensure updated global optimal powertrain control. In this work, we use genetic algorithm (GA) for long-term global optimization. The details of GA is discussed in the following section.

3) Genetic Algorithm for Global Optimization: Due to the non-differentiable and discontinuous nature of the global optimization formulation in (15), we employ GA in this work for fast and efficient global search for long-term global optimization. GA aims at solving both constrained and unconstrained optimization problems by iteratively modifying a population of individual solutions. Lower/upper boundaries and linear functions to produce new individuals at every generation. Only feasible new points are generated with respect to the linear and bound constraints. Once the optimal powertrain control is obtained, we can easily reconstruct the corresponding speed profile using:

$$V_{opt} = \sqrt{AX(0) + BU_{opt} + CD}$$

(16)

C. Local Adaption

While following the predetermined global reference speed profile $V_{opt}$, we should also consider local unpredictable perturbations, e.g., a sudden change of lane of vehicles on adjacent lane or a sudden slowdown of the preceding vehicle, to ensure safety driving distance. To account for local perturbations on the road, we propose a local adaptation technique that detects the distance from the preceding vehicle at real time, and adapt local speed profile if necessary to ensure safety distance.

Fig. 5 illustrates the local speed adaption flow based on real-time preceding vehicle speed, computed safety distance, and global optimal speed profile. The local speed adaption is performed on a time-based driving cycle, i.e., adaption is repeatedly performed at every time step $\Delta t$, usually very small, to ensure safety driving distance. At $i$-th time step, the distance from the preceding vehicle, denoted by $d_i$ as well as that from the preceding vehicle on the adjacent lane, denoted by $d_{i,adj}$ are computed. Note that $d_i$ and $d_{i,adj}$ can be measured and estimated by in-vehicle sensing devices such as image sensors, laser radar, and millimeterwave radar. The safety distance $\Delta D_t$ at $i$-th time step $t_i$ can be then computed based on the current vehicle speed:

$$\Delta D_t = h \times v(t_i) + l$$

(17)

where $h$ and $l$ are constants whose values can be set to 2 according to [30] and $v(t_i)$ is the instantaneous speed at time $t_i$. Based on the computed safety distance, we set a threshold distance $d_{follow}$ such that if $d_i \geq d_{follow}$, then we consider the vehicle is in safe mode and the speed at time step $t_i$ should follow the optimized global speed $V_{opt,i}$, which is obtained by a simple distance-to-time speed profile conversion. Meanwhile, the distance from the preceding vehicle on the adjacent lane $d_{i,adj}$ is also detected. If $d_i < d_{follow}$ and $d_{i,adj} \geq d_{follow}$, then the vehicle will change from the current lane to the adjacent lane and follow the optimized global speed $V_{opt,i}$. Note that in this work, we assume one adjacent lane, and this method can be easily extended to the case of 2 adjacent lanes. An example of lane change situation is illustrated in Fig. 6(a). If $d_i < d_{follow}$ and $d_{i,adj} < d_{follow}$, then there is a risk of safety distance violation given that the current distance is closer to $\Delta D_t$. In this case, we perform local optimization using optimized global speed profile as target and $\Delta D_{t+1}$ as additional constraints for safety distance. As shown in [30], by neglecting constant terms and terms with small variations, the cost function in local optimization can be expressed as the following quadratic notation:

$$J_{cost,i} = w_1 \cdot K \cdot u(i) + w_2 \cdot (u(i)^T B(i)^T B(i) u(i)) - 2B(i) u(i) \cdot V_{opt,i}^2$$

(18)
where \( w_1 \) and \( w_2 \) are weight values associated with each optimization goal, and \( K \) is the vector defined as \( K = [\hat{d}_i, \hat{d}_{i,adj}]^T \hat{v}_m \). Thus local optimization can be expressed as quadratic programming form:

\[
\min_{U(i)} w_2 \cdot u(i)^T B(i)^T B(i) u(i) + [w_1 K - 2w_2 B(i) V_{opt,i+1}] u(i)
\]

subject to \( 0 \leq u(i) \leq u_{i,max} \)

\[
B(i) u(i) \leq v_{max} - A(i) X(i) + D(i)
\]

where \( u_{i,max} \) is the upper boundary for \( u_i \), \( v_{max} \) denotes the maximum speed allowed at time \( i+1 \) to ensure safety driving distance

\[
v_{max} = \left( \Delta D(i+1)^s - l \right) / h
\]

where \( \Delta D(i+1)^s \) denotes the estimated spacing at time \( i+1 \) based on current spacing and current speed for both vehicles by assuming constant acceleration for the preceding vehicle:

\[
\Delta D(i+1)^s = \Delta D + \left( \frac{v_{pre}(i) + v_{pre}(i+1)}{2} - v(i) \right) \cdot \Delta t
\]

where \( v_{pre}(i) \) denotes the speed of the preceding vehicle at time \( i \).

Based on the above local speed adaption flow, we can define a vehicle status indicator \( o_{st} \) at each adaption for tracking the vehicle status throughout the local adaption process

\[
o_{st} = \begin{cases} 
1, & \text{if } d_i \geq d_{follow} \\
2, & \text{if } d_i < d_{follow} \text{ and } d_{i,adj} \geq d_{follow} \\
3, & \text{if } d_i < d_{follow} \text{ and } d_{i,adj} < d_{follow} \text{ and } o_{si} = 1 \\
4, & \text{if } d_i < d_{follow} \text{ and } d_{i,adj} < d_{follow} \text{ and } o_{si} = 0 \text{ and } o_{sadj} = 1 \\
5, & \text{if } d_i < d_{follow} \text{ and } d_{i,adj} < d_{follow} \text{ and } o_{si} = 0 \text{ and } o_{sadj} = 0
\end{cases}
\]

where \( o_{si}/o_{sadj} \) is the indicator parameter to denote if the local optimization is solvable at the current/adjacent lane.

The local optimization described in (19) has the standard form of quadratic programming, which can be solved using commonly used methods such as interior point method. This form significantly reduces computational complexity of local optimization. As can be shown in [33], quadratic programming can be efficiently implemented using a high-throughput Field-Programmable Gate Array (FPGA) with operating frequency over 100MHz and a typical chip size of 30 cm².

However, local optimization may fail to converge under some specific circumstances, e.g., a sudden change of lane from a vehicle on the adjacent lane without considering safety distance on the current lane. In such case, we need to force the vehicle to slow down to avoid collision. As shown in Fig. 5, when local optimization is unsolvable on the current and adjacent lanes, then we will force the vehicle to brake by imposing \( V_{local}(i+1) = \max(0, V_{pre}(i+1) - V_m) \), where \( V_m \) is a user-defined parameter to ensure the distance from preceding vehicle increases at the next time step: \( 0 \leq V_m \leq V_{pre}(i+1) \). The selection of \( V_m \) is a tradeoff between fuel consumption and safety. A smaller value of \( V_m \) will result in less fuel consumption in the emergent braking process while a larger value of \( V_m \) will result in larger distance at the expense of increasing fuel consumption. An example of brake situation is illustrated in Fig. 6(b).

IV. NUMERICAL EXAMPLE

The proposed ecological driving system for CAV using the proposed control hierarchy was illustrated based on simulation analysis in VISSIM. Recognizing the fact that a simulated network can truly reflect the reality only if it is well calibrated, we collected the field data at MD 100, Maryland and conducted a calibration for the VISSIM network. By observing the data at the study site of Maryland, the moderate traffic scenarios (10-20 vehicles/km/lane) in which the proposed model is more applicable usually happen after the peak-periods and can last about 1.5 hours. So the percentage of time for moderate traffic is around 12.5% (3 hours per day). For simulating the on-line operational procedure, we used the VISSIM-COM interface to develop a program to execute the local adaption function using VB.NET and the MYSQL database. During the simulation, the program detects and records the real-time traffic information and then adjusts the target vehicle’s trajectory. The road condition and vehicle parameters used in our study are the following: \( S = 5000m \), \( \Delta S = 25m \), \( n = 200 \), \( T_{max} = 220Nm \), \( F_{max} = 3120N \), \( f_r = 8 \), \( N_{fr} = 0.9 \), \( r_w = 0.25m \), \( m = 3000kg \), \( g = 9.8m/s^2 \), \( C_r = 0.01 \), \( \rho = 1.225 \), \( C_d = 0.3 \), \( A_d = 0.5m^2 \), \( \theta(t) = 0 \). We set \( w_1 = 10^8 \) and \( w_2 = 1 \) which give the best balance between driving time and fuel consumption [30]. The speed limit of the considered distance is set to \( 90km/h = 25m/s \). We predicted our traffic state (speed and density) using the macroscopic model and the rolling-horizon control logic as described in Section III-A. The predicted traffic speed is then smoothed and used as target speed profile for long-term optimization. The blue curve in Fig. 7 shows the traffic speed \( V(s,t,i) \), \( i = 1,...,200 \) predicted by our macroscopic model for the entire considered 200 segments. We then smoothed \( \hat{V}(s,t) \) using a Gaussian-weighted moving average filter to produce a more realistic and trackable traffic speed profile \( V_s \), as shown by the orange curve in Fig. 7, which will be used as the new smoothed target speed profile in our global optimization.

A. Long-Term Optimization Using GA

Once traffic speed is predicted, we perform long-term optimization using GA as shown in (15) by setting \( V_{max}(s,t) = \hat{V}(s,t) + 1.39m/s \) and \( V_{min}(s,t) = \hat{V}(s,t) - 1.39m/s \) to ensure that the vehicle is at most 1.39m/s = 5km/h different from the current average traffic in order not to block the traffic. The two red curves in Fig. 7 represents the speed boundaries \( V_{min}(s,t) \) and \( V_{max}(s,t) \) using \( V_{opt} \) as target speed profile. The long-term optimization is then performed as described in Section III-B. The initial optimal speed \( V_{opt}(0) \) is set to be equal to \( \hat{V}(0) \). Once the optimization is performed and
When $U_{opt}$ is computed, the global speed profile $V_{opt}$ is computed as specified in (16).

The green curve in Fig. 7 shows the optimized global speed profile $V_{opt}$ obtained by long-term optimization result $U_{opt}$. It can be observed that the optimal global speed profile is within our upper/lower boundaries shown by the red curves, and it generally follows the smoothed predicted traffic speed profile shown be the orange curve. Fig. 8 shows the vehicle powertrain parameters $\omega_e$ and $T_e$, brake force $F_{brake}$, and gear number profiles plotted as a function of distance steps as a result of global optimization. Fig. 9 shows the GA performance plot with green dots representing the best fitness values in each GA generation and blue dots representing the mean fitness values. The GA achieved convergence after 160 generations, and the total computing time for GA in global optimization is 28s for an Intel Xeon CPU at 3.4GHz and a RAM of 32GB.

To provide a more accurate estimation of the fuel consumption using the proposed approach, we have used a fuel map generated from Autonomie to compute the fuel consumption. Fig. 10 shows a comparison of fuel maps computed using Willans line model (dashed curve) and Autonomie (solid curve) as shown in [30]. It can be observed that the Willans line model curve generally follows well the one obtained from Autonomie. The 2nd column of Table II shows the fuel consumption, traveling time, and average speed obtained from the proposed approach using Willans line model, and the 3rd column shows the results using Autonomie fuel map based on the optimized powertrain parameters from global optimization. It can be observed that the resulted fuel consumption are very close to each other with an error of 0.7%, which justifies the use of approximated Willans line model in our approach. For the rest of the paper, the fuel consumption results are calculated from Autonomie fuel map.

To compare the effectiveness of the proposed approach with state-of-the-art methods, we used the Gipps’ car following...
model for all other vehicles during the trip in the VISSIM simulator, and we randomly selected 20 vehicles from the generated traffic in the simulator and recorded the speed profiles of these vehicles in the same 5000m traveling distance to compute the fuel consumption. For comparison purpose, we assume that all the 20 selected vehicles have the same powertrain model as the one under study.

The 4th column in Table II shows the average result from the 20 randomly selected vehicles as discussed before. It can be observed that our long-term optimization provides smaller fuel consumption as compared to the average value of the 20 selected vehicles. In order to show the statistical significance of this fuel saving, we performed a two-sample one-tailed t-test by considering the null hypothesis that the average fuel consumption of the 20 selected vehicles is equal to the value obtained using the proposed approach. The t-test result suggested that this null hypothesis is rejected at 5% significance level, which confirmed that the fuel consumption incurred from the proposed approach is smaller than other vehicles on the same trip with statistical significance.

We also made a comparison with the approach presented in [15], where powertrain parameters $T_e$ and $o_e$ are selected such that the fuel consumption rate $\dot{m}_{\text{fuel}}$ is minimized while the speed constraints are respected at each segment. The 5th column of Table II shows the result obtained using the approach in [15]. It can be observed that our long-term global optimization model provides the smallest fuel consumption with comparable average speed. The comparison results from Table II justify the need for optimizing target profile in the long-term global optimization.

### B. Local Adaption Results

1) **Local Adaption Using Optimized Global Speed Profile**

Once the optimized global speed profile $V_{opt}$ is obtained from the long-term global optimization, we then perform local adaption as described in Section III-C. We set the local adaption time step $\Delta t = 1s$, i.e., local adaption is repeated every 1s, and the safety distance threshold $d_{\text{follow}} = 50m$.

In addition to the predicted traffic flow, at every time step, we insert a lane change probability for each of the considered vehicle. As demonstrated in [34], the probability of driver’s discretionary lane change can be modeled by a binary logit model as a function of explanatory variables affecting decision and a random variable with normal distribution. Based on the empirical estimation from [34] and without loss of generality, we insert a discretionary lane change probability of 0.01.

![Fig. 11. Local adaption results: (a) local adapted speed profile and (b) vehicle status and lane information.](image)

Since local adaption is performed in time scale, the results are shown in time-scale in Fig. 11. The blue curve in Fig. 11(a) shows the local adapted speed profile and the red curve shows the target optimized global speed profile $V_{opt}$ in time scale. It can be observed that local speed profile has several abrupt speed reductions. To gain some insight about these reductions, the blue curve in Fig. 11(b) shows the vehicle status indicator value $v_{st}$ as defined by (22) and the green curve shows the lane number on which the vehicle travels at each time point. By combining Fig. 11(a) and (b), it can be observed that abrupt speed reductions mainly occur when the vehicle status information is 5, i.e., the distance from the preceding vehicle is less than $d_{\text{follow}}$ and local optimization is unsolvable for both lanes. Thus, the vehicle has to brake to avoid collision as described in Section III-C. When the distance from the preceding vehicle becomes greater than $d_{\text{follow}}$ or local optimization becomes solvable, our local adaption can quickly adapt the local speed to global optimal speed profile, which ensures minimum fuel consumption while keeping the safety driving distance.

The 2nd column of Table III shows the updated fuel consumption and traveling time information using local adapted speed profile shown by the blue curve in Fig. 11(a).

<table>
<thead>
<tr>
<th>Proposed with Willans line model</th>
<th>Proposed with fuel map from Autonomie</th>
<th>Average traffic</th>
<th>Approach in [15]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fuel consumption (kg)</td>
<td>0.28</td>
<td>0.278</td>
<td>0.29</td>
</tr>
<tr>
<td>Traveling time (s)</td>
<td>246</td>
<td>246</td>
<td>242</td>
</tr>
<tr>
<td>Average speed (m/s)</td>
<td>20.3</td>
<td>20.3</td>
<td>20.6</td>
</tr>
</tbody>
</table>

![Table II: Global Fuel Consumption and Traveling Time Comparison](image)

![Table III: Fuel Consumption Comparison for Local Adaption](image)
TABLE IV
FUEL CONSUMPTION VALUES AND DRIVING TIMES
FOR DIFFERENT $w_2$ VALUES WITH $w_1 = 10^8$

<table>
<thead>
<tr>
<th>$w_2$</th>
<th>Fuel consumption (kg)</th>
<th>Traveling time (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$w_3 = 0.5$</td>
<td>0.34</td>
<td>251</td>
</tr>
<tr>
<td>$w_3 = 1$</td>
<td>0.34</td>
<td>251</td>
</tr>
<tr>
<td>$w_3 = 5$</td>
<td>0.36</td>
<td>250</td>
</tr>
</tbody>
</table>

By comparing the 2nd column of Table III to the 2nd column of Table II, it can be observed that the fuel consumption from local speed profile is slightly higher than that obtained from optimized global speed profile, due to the abrupt speed reductions discussed before. The 3rd column in Table III shows the average local adaption results from the 20 randomly selected vehicles as discussed before. It can be observed that our approach still provides smaller fuel consumption as compared to the average value of the 20 selected vehicles in the local adaption.

As shown in (19), the choice of $w_1$ and $w_2$ is a tradeoff between the fuel consumption and how close the resulting speed profile is to the optimized global speed. Table IV shows different fuel consumption values and driving times for different $w_2$ values with $w_1$ fixed at $10^8$. It can be observed that since the number of times when local adaption is needed during the trip is relatively small, the impact of $w_1$ and $w_2$ on the final fuel consumption and driving time is limited.

C. Comparison With Global Target Profile Based on Smoothed Average Traffic

In order to illustrate the advantages of using predicted traffic flow as global speed profile, we have performed local adaption using the smoothed average traffic profile as shown by the orange curve in Fig. 7 as the global target profile. The 5th column of Table III shows the results based on smoothed average traffic profile. It can be observed that the fuel consumption using smoothed average traffic profile has a slightly higher fuel consumption as compared to the proposed approach with comparable traveling speed. Fig. 12 shows the local adaptation results based on smoothed average traffic profile. The red curve in Fig. 12(a) is the time-domain equivalent speed profile of the orange curve in Fig. 7, and the blue curve in Fig. 12(a) shows the adapted local speed profile. The vehicle status indicator and lane information are shown in Fig. 12(b).

D. Comparison With Single-Lane Optimization

One of the major contributions of the proposed approach is the consideration of lane change during optimization. To illustrate the significance of considering lane change, we have performed optimization in a single lane without lane change function. Fig. 13 shows local adaption results without lane change function. As can be observed, more abrupt speed reductions are observed as compared to Fig. 11. The fuel consumption after local adaption based on single-lane optimization is 0.38 kg. This result shows that single-lane optimization consumes more fuel, corroborating the necessity of developing lane change function in the optimization.

E. Road Grade Sensitivity Analysis

The final fuel consumption for the given traveling distance is impacted by several environmental and vehicular factors, including road grade, rolling resistance coefficient, vehicle mass, etc. The road grade parameter $\theta$ was set to 0 previously. To show how fuel consumption is impacted by $\theta$, we have performed a road grade sensitivity analysis. As demonstrated in [35], the road grade can be accurately modeled by a piecewise linear model. Thus, for the purpose of this study and without loss of generality, we employed a piecewise linear model composed of two linear functions with opposite slope.
values ranging from 0 to observe how fuel consumption varies as a function of the generated grade curve by adding a constant to the curve. The mean value (in degree) of distance steps. The mean value of the grade curve in Fig. 14 is plotted in degree as a function of to represent road grade variation throughout the trip. The grade signs and random Gaussian noise as illustrated in Fig. 14, to represent road grade variation throughout the trip. The grade curve shown in Fig. 14 is plotted in degree as a function of distance steps. The mean value of the grade curve in Fig. 14 is set to 0. We then adjusted the mean value (in degree) of the generated grade curve by adding a constant to the curve to observe how fuel consumption varies as a function of mean grade value.

Fig. 15 shows the fuel consumption for different grade mean values ranging from 0° to 5°. It can be observed that more fuels are consumed as the road becomes steeper, and the fuel consumption difference can be 0.29[kg] between 0° and 5° mean grade values. This observation justifies the consideration of road grade information in the fuel consumption computation model.

V. CONCLUSIONS

In this work, we proposed a two-stage hierarchical framework for minimizing fuel consumption in a CAV environment. Our proposed framework included traffic state prediction, global target speed optimization and local speed adaption. The predicted traffic state served as the target speed in the optimization process and the optimization function was activated once new traffic state predictions were available. The second stage, local speed adaption was designed to dynamically adjust vehicle speed and make lane-changing decision based on local driving conditions. The experimental results confirmed the effectiveness of the proposed system in reducing fuel consumption. Further comparisons with different models also highlighted the need of considering traffic state information in the first-stage optimization and lane-changing decision module in the local adaption function.

REFERENCES


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